

Centre No.					
Candidate No.					

Paper Reference					
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Surname	Initial(s)
Signature	

Paper Reference(s)

4400/3H

**London Examinations IGCSE
Mathematics**

Paper 3H

Higher Tier

Monday 10 May 2004 – Morning

Time: 2 hours

Examiner's use only

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Team Leader's use only

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Page Numbers	Leave Blank
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
Total	

Materials required for examination

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Items included with question papers

Nil

Instructions to Candidates

In the boxes above, write your centre number and candidate number, your surname, initial(s) and signature.

The paper reference is shown at the top of this page. Check that you have the correct question paper. Answer **ALL** the questions in the spaces provided in this question paper. Show all the steps in any calculations.

Information for Candidates

There are 20 pages in this question paper. All blank pages are indicated. The total mark for this paper is 100. The marks for parts of questions are shown in round brackets: e.g. (2). You may use a calculator.

Advice to Candidates

Write your answers neatly and in good English.

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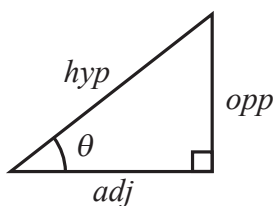
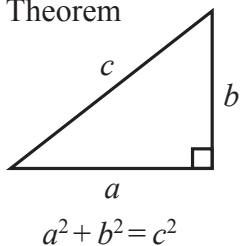
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Turn over



IGCSE MATHEMATICS 4400
FORMULA SHEET – HIGHER TIER

Pythagoras' Theorem

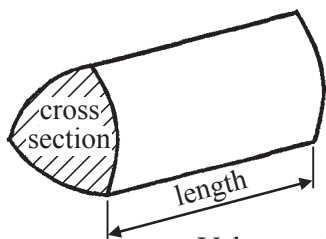


adj = hyp \times cos θ
opp = hyp \times sin θ
opp = adj \times tan θ

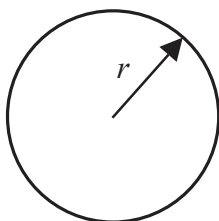
or $\sin \theta = \frac{\text{opp}}{\text{hyp}}$

$\cos \theta = \frac{\text{adj}}{\text{hyp}}$

$\tan \theta = \frac{\text{opp}}{\text{adj}}$

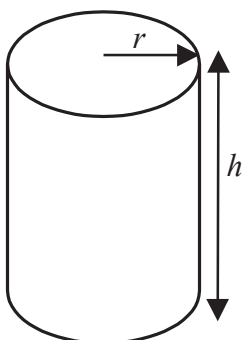


Volume of prism = area of cross section \times length



Circumference of circle = $2\pi r$

Area of circle = πr^2

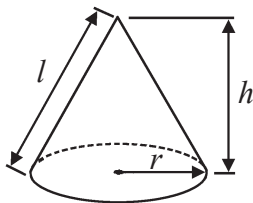


Volume of cylinder = $\pi r^2 h$

Curved surface area of cylinder = $2\pi r h$

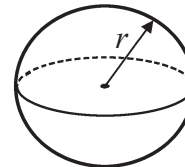
Volume of cone = $\frac{1}{3} \pi r^2 h$

Curved surface area of cone = $\pi r l$

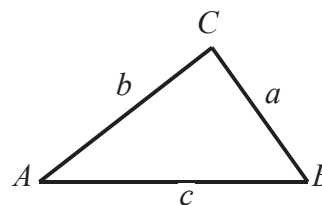


Volume of sphere = $\frac{4}{3} \pi r^3$

Surface area of sphere = $4\pi r^2$



In any triangle ABC

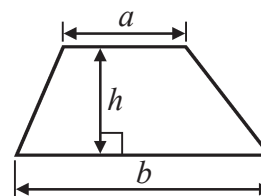


Sine rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle = $\frac{1}{2} ab \sin C$

Area of a trapezium = $\frac{1}{2} (a + b) h$



The Quadratic Equation
The solutions of $ax^2 + bx + c = 0$
where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Answer ALL TWENTY questions.

Leave
blank

Write your answers in the spaces provided.

You must write down all stages in your working.

1. In July 2002, the population of Egypt was 69 million.
By July 2003, the population of Egypt had increased by 2%.

Work out the population of Egypt in July 2003.

..... million

Q1

(Total 3 marks)

2. (a) Expand $3(2t + 1)$

.....
(1)

- (b) Expand and simplify $(x + 5)(x - 3)$

.....
(2)

- (c) Factorise $10p - 15q$

.....
(1)

- (d) Factorise $n^2 + 4n$

.....
(1)

Q2

(Total 5 marks)

3.

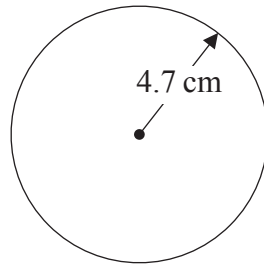


Diagram **NOT**
accurately drawn

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A circle has a radius of 4.7 cm.

- (a) Work out the area of the circle.
Give your answer correct to 3 significant figures.

..... cm²
(2)

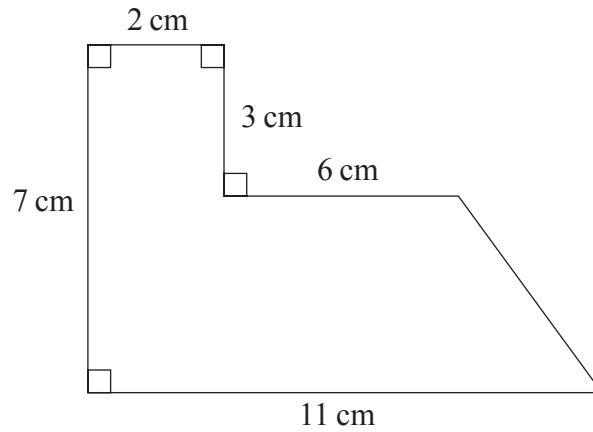


Diagram **NOT**
accurately drawn

The diagram shows a shape.

- (b) Work out the area of the shape.

..... cm²
(4)

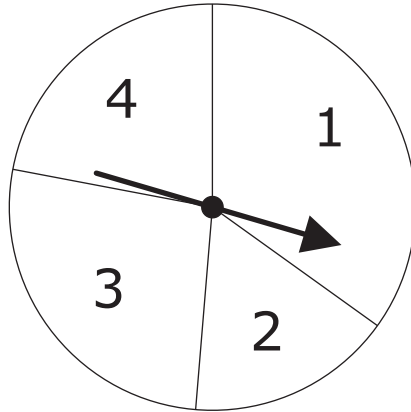
Q3

(Total 6 marks)

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4. The diagram shows a pointer which spins about the centre of a fixed disc.

*Leave
blank*



When the pointer is spun, it stops on one of the numbers 1, 2, 3 or 4.
The probability that it will stop on one of the numbers 1 to 3 is given in the table.

Number	1	2	3	4
Probability	0.35	0.16	0.27	

Magda is going to spin the pointer once.

- (a) Work out the probability that the pointer will stop on 4.

.....
(2)

- (b) Work out the probability that the pointer will stop on 1 or 3.

.....
(2)

Omar is going to spin the pointer 75 times.

- (c) Work out an estimate for the number of times the pointer will stop on 2.

.....
(2)

Q4

(Total 6 marks)

5. (a) Express 200 as the product of its prime factors.

Leave
blank

.....
(2)

(b) Work out the Lowest Common Multiple of 75 and 200.

.....
(2)

Q5

(Total 4 marks)

6. Two points, A and B , are plotted on a centimetre grid.
 A has coordinates (2, 1) and B has coordinates (8, 5).

(a) Work out the coordinates of the midpoint of the line joining A and B .

(..... ,)
(2)

(b) Use Pythagoras' Theorem to work out the length of AB .
Give your answer correct to 3 significant figures.

..... cm
(4)

Q6

(Total 6 marks)

7. $A = \{1, 2, 3, 4\}$
 $B = \{1, 3, 5\}$

Leave blank

(a) List the members of the set

(i) $A \cap B$,

(ii) $A \cup B$.

.....

.....
(2)

(b) Explain clearly the meaning of $3 \in A$.

.....

(1)

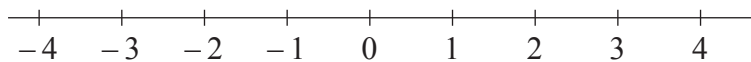
Q7

(Total 3 marks)

8. (i) Solve the inequality $3x + 7 > 1$

.....

(ii) On the number line, represent the solution to part (i).



Q8

(Total 4 marks)

9. The grouped frequency table gives information about the distance each of 150 people travel to work.

Leave blank

Distance travelled (d km)	Frequency
$0 < d \leq 5$	34
$5 < d \leq 10$	48
$10 < d \leq 15$	26
$15 < d \leq 20$	18
$20 < d \leq 25$	16
$25 < d \leq 30$	8

- (a) Work out what percentage of the 150 people travel more than 20 km to work.

..... %
(2)

- (b) Work out an estimate for the mean distance travelled to work by the people.

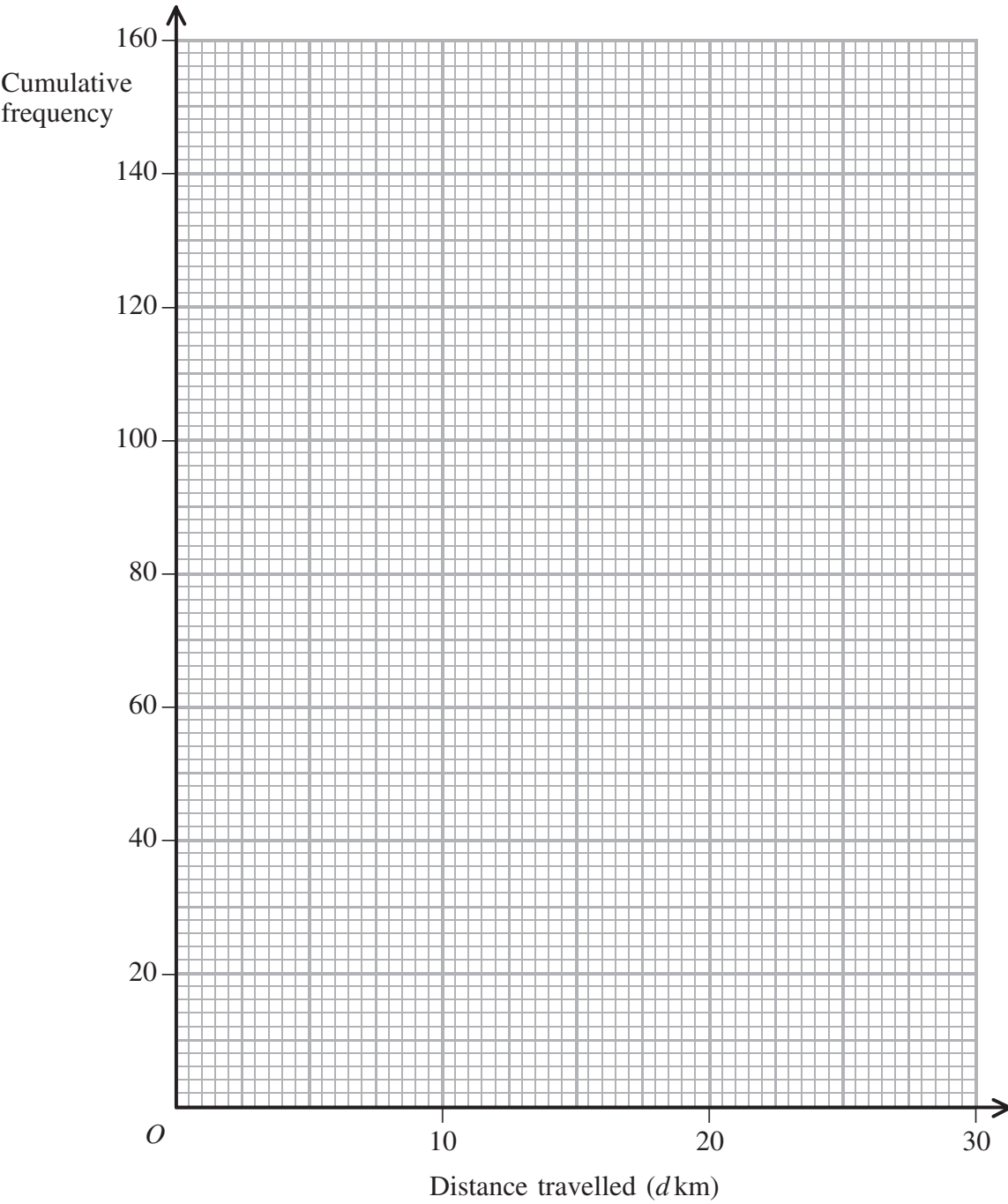
..... km
(4)

- (c) Complete the cumulative frequency table.

Distance travelled (d km)	Cumulative frequency
$0 < d \leq 5$	
$0 < d \leq 10$	
$0 < d \leq 15$	
$0 < d \leq 20$	
$0 < d \leq 25$	
$0 < d \leq 30$	

(1)

Leave blank



- (d) On the grid, draw a cumulative frequency graph for your table. (2)
- (e) Use your graph to find an estimate for the median of the distance travelled to work by the people.
Show your method clearly.

..... km
(2)

Q⁹

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(Total 11 marks)

10.

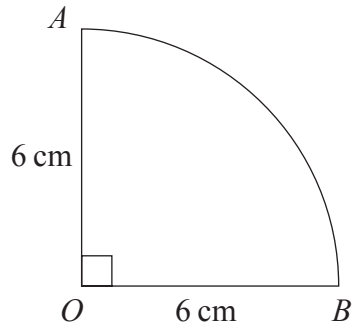


Diagram **NOT** accurately drawn

Leave blank

The diagram shows a shape.
 AB is an arc of a circle, centre O .
 Angle $AOB = 90^\circ$.
 $OA = OB = 6$ cm.

Calculate the perimeter of the shape.
 Give your answer correct to 3 significant figures.

..... cm

Q10

(Total 4 marks)

11. The distance between the Earth and the Sun is 150 000 000 km.

(a) Write the number 150 000 000 in standard form.

.....

(1)

The distance between Neptune and the Sun is 30 times greater than the distance between the Earth and the Sun.

(b) Calculate the distance between Neptune and the Sun.
 Give your answer in standard form.

..... km

(2)

Q11

(Total 3 marks)

12. (a) Find the gradient of the line with equation $3x - 4y = 15$

Leave
blank

.....
(3)

(b) Work out the coordinates of the point of intersection of the line with equation $3x - 4y = 15$ and the line with equation $5x + 6y = 6$

(.....,)
(4)

Q12

(Total 7 marks)

13. A body is moving in a straight line which passes through a fixed point O .
The displacement, s metres, of the body from O at time t seconds is given by

$$s = t^3 + 4t^2 - 5t$$

(a) Find an expression for the velocity, v m/s, at time t seconds.

$v =$
(2)

(b) Find the acceleration after 2 seconds.

..... m/s^2
(2)

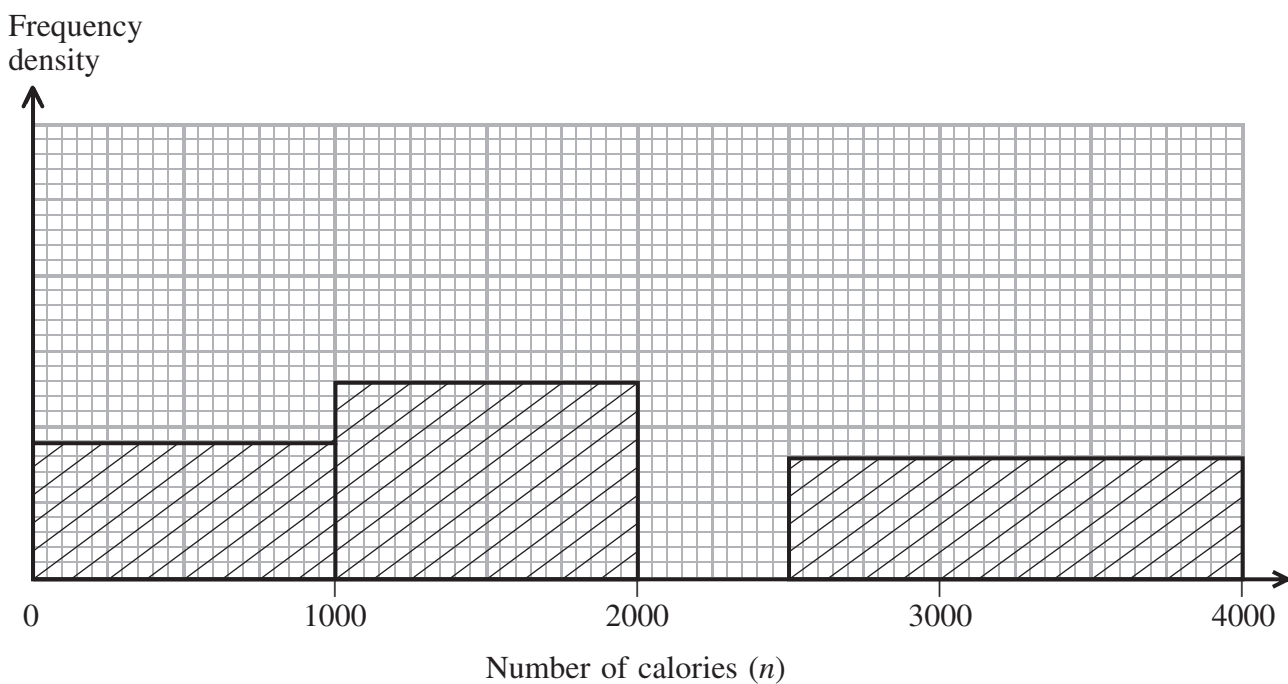
Q13

(Total 4 marks)

14. The unfinished table and histogram show information from a survey of women about the number of calories in the food they eat in one day.

Leave blank

Number of calories (n)	Frequency
$0 < n \leq 1000$	90
$1000 < n \leq 2000$	
$2000 < n \leq 2500$	140
$2500 < n \leq 4000$	



(a) (i) Use the information in the table to complete the histogram.

(ii) Use the information in the histogram to complete the table.

(3)

(b) Find an estimate for the upper quartile of the number of calories.
You must make your method clear.

(2)

Q14

(Total 5 marks)

15. The length of a side of a square is 6.81 cm, correct to 3 significant figures.

*Leave
blank*

(a) Work out the lower bound for the perimeter of the square.

..... cm
(2)

(b) Give the perimeter of the square to an appropriate degree of accuracy.
You must show working to explain how you obtained your answer.

..... cm
(2)

Q15

(Total 4 marks)

16. Express the algebraic fraction $\frac{2x^2 - 3x - 20}{x^2 - 16}$ as simply as possible.

Q16

.....
(Total 3 marks)

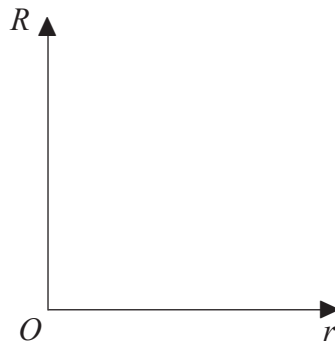
17. An electrician has wires of the same length made from the same material.
 The electrical resistance, R ohms, of a wire is inversely proportional to the square of its radius, r mm.
 When $r = 2$, $R = 0.9$

Leave blank

(a) (i) Express R in terms of r .

$R = \dots\dots\dots$

(ii) On the axes, sketch the graph of R against r .



(4)

One of the electrician's wires has a radius of 3 mm.

(b) Calculate the electrical resistance of this wire.

$\dots\dots\dots$ ohms
(1)

Q17

(Total 5 marks)

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18.

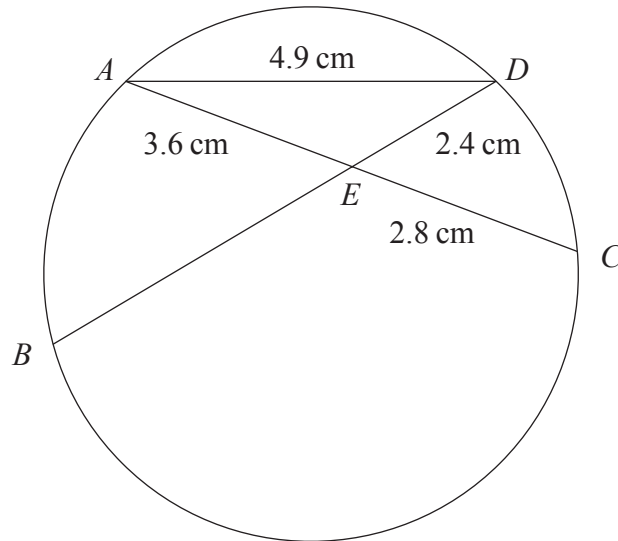


Diagram **NOT** accurately drawn

Leave blank

A, B, C and D are four points on the circumference of a circle.
The chords AC and BD intersect at E .
 $AE = 3.6$ cm, $CE = 2.8$ cm, $DE = 2.4$ cm and $AD = 4.9$ cm.

(a) Calculate the length of BE .

..... cm
(3)

(b) Calculate the size of angle AED .
Give your answer correct to 3 significant figures.

.....
(3)

Q18

(Total 6 marks)

19.

$$f: x \mapsto 2x - 1$$

$$g: x \mapsto \frac{3}{x}, x \neq 0$$

*Leave
blank*

(a) Find the value of

(i) $f(3)$,

.....

(ii) $fg(6)$.

.....
(2)

(b) Express the inverse function f^{-1} in the form $f^{-1}: x \mapsto \dots$

.....
(2)

(c) (i) Express the composite function gf in the form $gf: x \mapsto \dots$

.....

(ii) Which value of x must be excluded from the domain of gf ?

$x =$
(2)

Q19

(Total 6 marks)

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20.

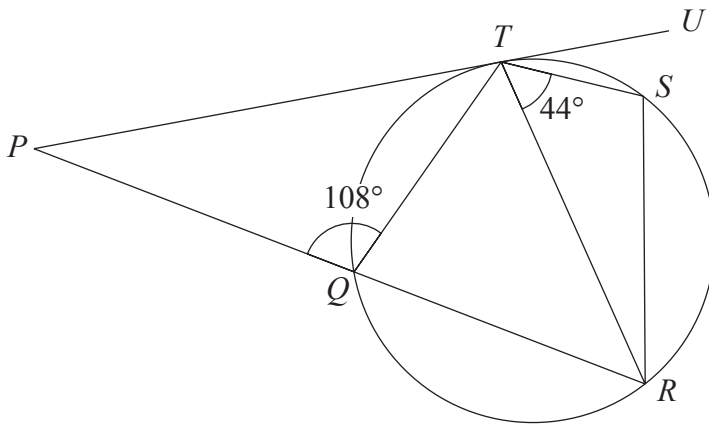


Diagram **NOT**
accurately drawn

Leave
blank

Q , R , S and T are points on the circumference of a circle.

PU is a tangent to the circle at T .

PQR is a straight line.

Angle $PQT = 108^\circ$.

Angle $STR = 44^\circ$.

Work out the size of angle STU .

You must give a reason for each step in your working.

.....
◦ Q20

(Total 5 marks)

TOTAL FOR PAPER: 100 MARKS

END