

Mark Scheme (Results) Summer 2010

IGCSE

IGCSE Mathematics (4400) Paper 3H Higher Tier



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Summer 2010 IGCSE Mathematics (4400) Mark Scheme - Paper 3H

Apart from Questions 4(c), 16 and 21 (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

	Q	Working	Answer	Mark		Notes
1	a	$\frac{15}{6}$ oe or $\frac{100}{6}$ oe inc value rounded or truncated to at least 1 dp eg 16.6, 16.7		2	M1	
			250		A1 cao	
	b	$\frac{900}{6}$ or $\frac{5}{6}$ oe inc value rounded or truncated to at least 2 dp eg 0.83		2	M1	
			750		A1 cao	
						Total 4 marks

2 ai	62	2	B1	cao
ii	alternate		B1	Accept 'opposite and corresponding' (need both)
				or 'opposite, angle sum of triangle = 180° and
				sum of angles on a line = 180°' (need all three)
bi	71	2	B1	cao
ii	corresponding		B1	Accept 'opposite and alternate' (need both)
				or 'opposite, angle sum of triangle = 180° and
				sum of angles on a line = 180°' (need all three)
				Total 4 marks

3 a	6	1	B1	cao
b	7	1	B1	cao
				Total 2 marks

	Q	Working	Answer	Mark		Not	es
4	a	-	5n + 30	1	B1		
	b		y ⁶	1	B1	cao	
	С	4x - 8 = 3		3	M1	for correct expansion of $4(x-2)$ or for either 4x = 3 + 2 or $4x = 5following 4x - 2 = 3$	M2 for $x - 2 = \frac{3}{4}$
		4x = 8 + 3 or 4x = 11	$2\frac{3}{4}$ oe		M1 A1	for $4x = 8 + 3$ or $4x = 11$ dep on 2 method mai	rks
			$\frac{2}{4}$ de		AI	dep on z method mai	
							Total 5 marks

5 a	$\frac{3}{10} \times \frac{5}{6}$		2	M1	
		$\frac{15}{60}$ or $\frac{1}{4}$		A1	Accept $\frac{3}{12}$, $\frac{5}{20}$
b		24	2	B2	B1 for multiple of 24
					Total 4 marks

	Q	Working	Answer	Mark		Notes
6	a	Ĭ.	400 < <i>V</i> < 500	1	B1	Accept 400-500
	b	50 × 2 + 150 × 4 + 250 × 6 + 350 × 18		4	M1	for finding at least 4 products
		+ 450 × 44 + 550 × 6				$m \times f$ consistently within
		= 100+600+1500+6300+19 800+3300				intervals (inc end points)
		= 31 600			M1	(dep) for use of at least 4 correct halfway values
		31 600 ÷ 80			M1	(dep on 1st M1) for adding and ÷ by 80
			395		A1	
	С		2 6 12 30 74 80	1	B1	cao
	d		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table
			Curve or line segments		B1	ft from points if 4 or 5 correct
						or if points are plotted
						consistently within each interval
		_				at the correct heights
	е	Use of 40 (or 40.5) on graph or 40		2	M1	for use of 40 (or 40.5) on cf graph
		(or 40.5) stated				or for 40 (or 40.5) stated
			approx 420		A1	If M1 scored, ft from cf graph
						If no indication of method, ft
						only from correct curve & if
						answer is correct
						(<u>+</u> ½ sq tolerance) award M1 A1
				-		Total 10 marks

Q	Working	Answer	Mark		Ŋ	Notes
7	cos and 41		3	M1	or M1 for	or M1 for correct
	6.8 cos 41°			M1	6.8sin41°	statement of
					(4.461) and	Sine Rule eg
					6.8^2 –	6.8 x
					"4.461" ²	$\frac{1}{\sin 90^{\circ}} = \frac{1}{\sin 49^{\circ}}$
					(26.337)	M1 for correct
					M1 for	expression for x
					$\sqrt{"26.337"}$	eg
						6.8 sin 49°
						$x = \frac{1}{\sin 90^{\circ}}$
		5.13		A1	for ans rounding t	o 5.13 (5.132025)
						Total 3 marks

8	$\frac{1786}{0.76}$ or $1786 \times \frac{100}{76}$ oe		3	M2	for $\frac{1786}{0.76}$ or $1786 \times \frac{100}{76}$ oe M1 for $\frac{1786}{76}$, $76\% = 1786$, $\frac{1786}{0.76} = 0.76$, $1786 = 0.76x$	
					x or 23.5 seen	
		2350		A1	cao	
						Total 3 marks

Q	Working	Answer	Mark		Notes	
9 a		reflection in the line $y = -x$	2	B2	B1 for reflection	These marks are
					B1 for $y = -x$ oe	independent
					[accept eg	but award no marks
					"in dotted line"	if the answer is not a
					or "in line through	single transformation
					(-5,5) and $(5, -5)$ "]	
b		R correct	2	B2	B1 for 2 vertices correct	
	,	Vertices are $(2,-1)(3,-1)(3,-3)$			or for a translation of R	
					or for a 90° clockwise ro	otation of Q about (-1,1)
С		reflection in the line $y = 1$	2	B2	B1 for reflection	As in (a)
					B1 for $y = 1$ oe	
					[accept eg "in a	
					horizontal line	
					through (0,1)]	
					ft from (b),	
					if B1 scored in (b)	
						Total 6 marks

10 a		-4 <u><</u> x < 3	2	B2	Also accept ' $x < 3$ and $x \ge -4$ '
					B1 for $-4 \le x \le 3$, $-4 < x < 3$,
					-4 < x ≤ 3, a double-ended inequality
					which is correct at one end
					(ignore the other end)
					Also award B1 for $x \ge -4$, $x < 3$,
					'x < 3 <u>or</u> x ≥ -4'
bi	2x > -8		4	M1	for 2x > - 8 or x + 4.5 > 0.5
		x > -4		A1	for $x > -4$ as final answer
ii		-3 -2 -1	2	B2	B1 for 3 correct and 1 wrong
					or for 2 correct and none wrong
					Total 6 marks

Q	Working	Answer	Mark		Notes
11 a	$\pi \times 8^2$		2	M1	
		201		A1	for ans rounding to 201
					$(\pi \to 201.061 \ 3.14 \to 200.96)$
b	eg 8.5870 × 587.71		2	M1	for correct evaluation of
					at least 2 of the terms inside
					the brackets (126.75, 192, 268.96
					accept if rounded or truncated to at least 3sf)
					or for correct evaluation of brackets
					(587.71 - accept 587, 588 or 587.7)
		5050		A1	Accept any answer
					in the range 5040-5050 inclusive.
					$(\pi \to 5046.677\ 3.14 \to 5044.119)$
					Total 4 marks

12 a		18 13 2 -9 -14	2	B2	for all correct
					B1 for 3 or 4 correct
b		Points	2	B1	$\pm \frac{1}{2}$ sq ft from (a) if at least B1 in (a)
		Curve		B1	ft if B1 awarded for points or if
					there is not more than
					one point incorrectly plotted and
					at least B1 scored in (a)
					Award for single curve (not line segments)
					which does not miss.
					more than one plotted point
					by more than ½ square
ci		$3x^2 - 12$	4	B2	B2 for $3x^2 - 12$
					B1 for two of three terms
					differentiated correctly
ii	$3 \times 5^2 - 12$			M1	for substn $x = 5$ in their (c)(i) if at least B1
					scored in (c)(i)
		63		A1	cao
			·		Total 8 marks

Q	Working	Answer	Mark	Notes		
13	There are 4 independent requirements to consider when marking this question but the order in which					
	they are satisfied wi	ll vary. Focus on these 4 key po	ints, igno	oring irre	elevant or incorrect statements.	
	$\angle PQS = 36^{\circ} \text{ or } \angle SPR = 54^{\circ}$		4	B1 May be stated or marked on diagram		
	angles in the same segment			B1	Award if 'same segment', 'same arc',	
					or 'same chord'	
	$\angle PQR = 90^{\circ} \text{ or } \angle PSR = 90^{\circ}$			B1 Angle may be stated or marked on diagram. Condone omission of 'is a right angle' oe.		
	and					
	angle in a semicircle is a right angle					
		54		B1	cao	
					Total 4 marks	

14	ai		15	2	B1	cao
	ii		8.25		B1	cao
	b	$\frac{1}{2}$ × "15" × "8.25"		2	M1	
			61.875		A1	Also accept 61.88
	С	"8.25"		3	M1	numerator "8.25"
					M1	denominator 25
			0.33		A1	cao
						Total 7 marks

Q	Working	Answer	Mark		Notes
15 a	$E = \frac{k}{r^2}$		3	M1	for $E = \frac{k}{r^2}$ but not for $E = \frac{1}{2}$
	$4 = \frac{k}{50^2}$			M1	but not for $E = \frac{1}{r^2}$
	30	$\frac{10000}{r^2}$		A1	Award 3 marks if answer is $E = \frac{k}{r^2}$
b		25	1	B1	but k is evaluated as 10 000 in any part ft from $\frac{"10000"}{400}$ except for $k = 1$, if at least M1 scored in (a)
С	$r^2 = \frac{10000}{1600}$ oe		2	M1	for substitution and rearrangement into form $r^2 = \frac{k}{1600} \text{ or } r = \frac{\sqrt{k}}{40} \text{ with their value of } k$ except for $k = 1$
		2.5 oe		A1	cao
					Total 6 marks

16	eg $9 - 3\sqrt{5} - 3\sqrt{5} + \sqrt{5}^2$	2	B2	B1 for $9 + \sqrt{5}^2$ or $9 + \sqrt{5}\sqrt{5}$
	$9-2\times3\sqrt{5}+\sqrt{5}^2$			or $9 + \sqrt{25}$ or $3^2 + \sqrt{5}^2$
				or $3^2 + \sqrt{5}\sqrt{5}$ or $3^2 + \sqrt{25}$
				B1 for $-3\sqrt{5} - 3\sqrt{5}$
				or for $-2 \times 3\sqrt{5}$
				Total 2 marks

Q	Working	Answer	Mark	Notes
17	$\frac{18}{12}$ or 1.5 oe or 18 : 12 oe		3	M1 for $\frac{18}{12}$ or 1.5 oe or 18 : 12 oe
				Also award for $\frac{12}{18}$ or $\frac{2}{3}$
				or 12 : 18 oe
	544 × 1.5 ²			M1 for 1.5^2 or 2.25 or $\frac{9}{4}$ or $9:4$ oe
				Also award for $\left(\frac{2}{3}\right)^2$ or $\frac{4}{9}$
				or 4:9 oe
		1224		A1 cao
				Total 3 marks

18	x(x+6)		3	B1	for $x(x + 6)$
	$\frac{x(x+6)}{(x+6)(x-6)}$				Accept (x + 0)(x + 6)
	(x + 0)(x - 0)			B1	for $(x + 6)(x - 6)$
		х		B1	cao
		${x-6}$			
					Total 3 marks

Q	Working	Answer	Mark		Notes	
19 a	$\frac{3}{6} \times \frac{3}{6}$		2	M1	for $\frac{3}{6} \times \frac{3}{6}$ oe	
		$\frac{9}{36}$ or $\frac{1}{4}$ oe		A1	Sample space method - award 2 marks for a correct answer, otherwise no marks	
b	$\frac{1}{6} \times \frac{5}{6} + \frac{2}{6} \times \frac{3}{6}$ or $\frac{1}{6} \times \frac{2}{6} + \frac{1}{6} \times \frac{3}{6} + \frac{2}{6} \times \frac{3}{6}$ or $\frac{3}{6} \times \frac{3}{6} + \frac{1}{6} \times \frac{2}{6}$		3	M1	for one of $\frac{1}{6} \times \frac{5}{6}$, $\frac{2}{6} \times \frac{3}{6}$, $\frac{1}{6} \times \frac{2}{6}$, $\frac{1}{6} \times \frac{3}{6}$, $\frac{3}{6} \times \frac{3}{6}$	SC M1 for one of $\frac{1}{6} \times \frac{2}{5}, \ \frac{1}{6} \times \frac{3}{5},$ $\frac{2}{6} \times \frac{3}{5}$
				M1	for sum of 2 or 3 products which, evaluated accurately, gives the correct answer	M1 for $ \frac{1}{6} + \frac{2}{6} \times \frac{3}{5} \text{ or} $ $ \frac{1}{6} \times \frac{2}{5} + \frac{1}{6} \times \frac{3}{5} $ $ + \frac{2}{6} \times \frac{3}{5} $
		11/36		A1	A1 Sample space method - award 3 marks for a correct answer, otherwise no marks. Accept 0.305, 0.30, 0.31, 0.305, 0.306 etc but not 0.3 Total 5 mark	

Q	Working	Answer	Mark		Notes
20	13° or 19° angle of elevation identified		6	B1	On diagram or implied by working
				M1	for 40 tan 13° or 9.2347
					rounded or truncated to at least 2 sf
					or any complete, correct method of finding
					the height of the flagpole
	$tan 19^{\circ} = \frac{"9.2347"}{BC}$			M1	or for $\tan 71^\circ = \frac{BC}{"9.2347"}$
	(BC) "9.2347" 40 tan 13°			M1	for correct expression for BC,
	$(BC =) \frac{"9.2347"}{\tan 19^{\circ}} \text{ or } \frac{40 \tan 13^{\circ}}{\tan 19^{\circ}}$				which need not be evaluated
	or 26.819				eg also accept 40 tan 13° tan 71°
					If evaluated, accept 26.7 or 26.8
					or any value which rounds to 26.7 or 26.8
					$(\frac{9.2}{\tan 19^{\circ}} \rightarrow 26.718$
					$\frac{9.23}{\text{tan19}^{\circ}} \rightarrow 26.805)$
	40 ² +"26.819" ²			M1	dep on first two M1s
					for 40 ² +"26.819" ²
					or for complete, correct method of
					finding length of AC
		48.2	2	A1	for ans rounding to 48.2
					(48.1590)
					Award 6 marks for an answer
					which rounds to 48.2,
					if it has been obtained
					by a mathematically correct method
					Total 6 marks

Q	Working	Answer	Mark	Notes
21	$2x^2 = 3x + 14$ May be implied by second M1		5	$y = 2\left(\frac{y-14}{3}\right)^2$
	$2x^2 - 3x - 14 = 0$			$M1 2y^2 - 65y + 392 = 0$
	$(2x-7)(x+2)(=0)$ or $\frac{3\pm\sqrt{121}}{4}$			M1 $(2y-49)(y-8)(=0)$
	or $\frac{3}{4} \pm \frac{\sqrt{121}}{4}$			or $\frac{65 \pm \sqrt{1089}}{4}$
				or $\frac{65}{4} \pm \frac{\sqrt{1089}}{4}$
		$x = \frac{7}{2}, x = -2$		A1 dep on all method marks
		2		$y = \frac{49}{2}$, $y = 8$
				A1 dep on all method marks
		$x = \frac{7}{2}, \ y = \frac{49}{2}$		$x = \frac{7}{2}, \ y = \frac{49}{2}$
		x = -2, y = 8		x = -2, y = 8
				Total 5 marks

Total 100 marks

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