

MATHEMATICS 4400, MARK SCHEME

Paper 3H

| Q | Working | Answer | Mark | Notes | Total marks |
|----|--|----------------|------|--|----------------------|
| 1. | $\frac{5.8}{3.12}$ | 1.8589... | 2 | M1 For 5.8 or 3.12 seen A1 For first 5 figures | Total 2 marks |
| 2. | $10x + 15 = 30$ or $2x + 3 = 6$ $10x = 30 - 15$ or $2x = 6 - 3$ | $1\frac{1}{2}$ | 3 | M1 For $10x + 15$ or $2x + 3 = 6$ M1 For isolating x term in $ax + b = c$ A1 For $1\frac{1}{2}$ oe inc $\frac{3}{2}$ | Total 3 marks |
| 3. | $\frac{15}{18} - \frac{8}{18}$ | $\frac{7}{18}$ | 2 | M1 For clear attempt to express with common denominator - at least one correct A1 cao | Total 2 marks |
| 4. | correct enlargement | | 3 | B3 B2: for translation of correct shape or 2 vertices correct B1: for one side correct length or for enlargement scale factor 2, centre (2,1) | Total 3 marks |

| | | | | | |
|----|-----|---------------------------------------|---|----------|---|
| 5. | (a) | $0.45 + 0.12$ | 2 | M1 | For $0.45 + 0.12$ or $1 - (0.45 + 0.12)$ or $1 - 0.45 - 0.12$ or 0.43 |
| | | 0.57 | | A1 | For 0.57 or as final answer |
| | (b) | 250×0.12 or 250×0.1 | 2 | M1 A1 | For 250×0.12 or 250×0.1 cao |

Total 4 marks

| | | | | | |
|----|-----|------------------|---|----|---|
| 6. | (a) | $3(3p + 5)$ | 1 | B1 | cao |
| | (b) | $q(q - 4)$ | 1 | B1 | cao |
| | (c) | $(x + 2)(x - 5)$ | 2 | B2 | (B1 for one correct factor or signs reversed) |

Total 4 marks

| | | | | | |
|----|-----|---------------------------------------|---|----------|-------------|
| 7. | (a) | $\left(\frac{9+5}{2}\right) \times 6$ | 2 | M1 | |
| | | 42 | | A1 | cao |
| | (b) | "42" x 15 | 2 | M1 A1 | ft from (a) |

Total 4 marks

| | | | | | | |
|----------------------|-----|---|---|----------------------|---|---------|
| 8. | (a) | eg $\frac{15}{100} \times 240$ or 36 $240 - "36"$ | 3 | M1 M1 A1 | Or M2 for $\frac{100-15}{100} \times 240$ dep on first M1 cao | 204 |
| | (b) | 0.85 oe seen $\frac{663}{0.85}$ | 3 | B1 M1 A1 | For $\frac{663}{0.85}$ or $\frac{663}{1-0.15}$ cao | 780 |
| Total 6 marks | | | | | | |
| 9. | (a) | $2x < 8$ | 2 | M1 A1 | For $x < 4$ as final answer | $x < 4$ |
| | (b) | | 2 | B2 | (B1 for two correct and none wrong or three correct and one wrong) | 1, 2, 3 |
| Total 4 marks | | | | | | |
| 10. | (a) | $15 \times 8 + 25 \times 38 + 35 \times 28 + 45$ $\times 4 + 55 \times 2$ $= 120 + 950 + 980 + 180 + 110$ $= 2340$ $2340 \div 80$ | 4 | M1 M1 M1 A1 | For products $m \times f$ where m is consistent inc end points (dep) for use of midpoints (15,25... or 15.5,25.5,...) (dep on 1 st M1) for adding and $\div 80$ Accept 29, 29.2, 29.3 if first two M1s scored (If 15.5,25.5... used, mean = $\frac{2380}{80} = 29.75$) | 29.25 |

| | | | | |
|-----|---|---|----------|--|
| (b) | 8, 46, 74, 78, 80 | 1 | B1 | cao |
| (c) | Points correct Curve or line segments | 2 | B1 B1 | $\pm\frac{1}{2}$ sq ft from sensible table ft from points if 4 or 5 points correct or if points are plotted consistently within each interval at the correct heights |
| (d) | use of 40 (or 40.5) on graph or 40 th (or 40.5 th) stated | 2 | M1 A1 | For use of 40 (or 40.5) on graph or 40 th (or 40.5 th) stated If M1 scored, ft from cumulative frequency graph If no working, follow through only from correct curve |
| -29 | | | | |
| 11. | $h^2 = \frac{W}{l}$ | 2 | M1 A1 | Total 9 marks |
| 12. | (a) 30 : 1200 or 1200 : 30 oe | 3 | M2 A1 | Total 2 marks |
| | 1 : 40 | | | For 30 : 1200 or 1200 : 30 oe [M1 for 12(00...) : 30(00...) or 30(00...) : 12(00...) oe] Accept 1 : 0.025, 1 : $\frac{1}{40}$ oe, $n = 40$ ft if M1 scored SC B2 for 1 : 2.5, 1 : 4, 1 : 0.4, 1 : 400, 1 : 25, 1 : 250 |

| | | | | | |
|----------------------|--|--|----------------|-------------------|-------------|
| (b) | $95 \times "40" \text{ or } 3800$ $"3800" \div 100$ | 38 | M1 M1 A1 | ft from their n | |
| OR | $\frac{95}{30}$ $\times 12$ | 38 | M1 M1 A1 | (dep) | |
| Total 6 marks | | | | | |
| 13. | (a) | $\frac{360}{18}$ | 2 | M1 | |
| | (b) | "20" $\times (180 - 18)$ or ("20" $- 2) \times 180$ | 20 | A1 A1 | cao |
| | | 3240 | 2 | M1 A1 | ft from (a) |
| Total 4 marks | | | | | |

| | | | | |
|-----|--|-----|----|---|
| 14. | $2(x-1) + 2x + 3 = 4$ <p>or $\frac{2(x-1) + 2x + 3}{4} = 1$</p> <p>or $\frac{2(x-1)}{4} + \frac{2x+3}{4} = 1$</p> $2x - 2 + 2x + 3 = 4$ <p>or $\frac{2x-2+2x+3}{4} = 1$</p> <p>or $\frac{2x-2}{4} + \frac{2x+3}{4} = 1$</p> $4x = 3$ | 4 | M1 | <p>Clear attempt to multiply both sides by 4 (or multiple) or expressing LHS with a denominator of 4 or a multiple of 4</p> <p>(dep) expanding brackets</p> <p>or M2 for $\frac{x}{2} - \frac{1}{2} + \frac{2x}{4} + \frac{3}{4} = 1$ (M1 if one error)</p> <p>(dep on first M1) reducing to form $ax = b$ using a correct method</p> <p>or $\frac{x}{2} + \frac{2x}{4} = 1 + \frac{1}{2} - \frac{3}{4}$</p> <p>oe</p> |
| | | 3/4 | A1 | Total 4 marks |
| 15. | (a) $\frac{10\sqrt{5}}{\sqrt{5} \times \sqrt{5}}$ | 2 | M1 | Accept $10 = k5$ or $\sqrt{20}$ |
| | (b) $25 + (5\sqrt{3}) + (5\sqrt{3}) + (\sqrt{3})^2$ | 2 | A1 | Accept $k = 2$ |
| | $28 + 10\sqrt{3}$ | 2 | M1 | Accept $a = 28, b = 10$ |
| | | | A1 | Total 4 marks |

| | | | | | |
|-----|--|----------------------|---|----------------|---|
| 16. | (a) Angle of elevation identified 50 tan 19° | | 3 | B1 M1 A1 | On diagram or implied by working 17.2 or better (17.2163...) |
| | (b) $50^2 + 27^2$ or 56.8(2...) or $50^2 + "17.2"$ or value rounding to 52.88.. $\sqrt{"56.8"} + "17.2"$ or $\sqrt{"52.9"} + 27^2$ | 17.2 | 3 | M1 | |
| | | 59.3 - 59.4 | | A1 | For 59.3 - 59.4 |
| | | | | | Total 6 marks |
| 17. | (a) $(x + 4)(x + 1) - 15 = 35$ | | 3 | M1 | For $(x + 4)(x + 1) - 15 = 35$ or $(x + 1)(x + 4) = 50$ |
| | $x^2 + 5x + 4 - 15 = 35$ | $x^2 + 5x - 11 = 35$ | | B1 A1 | For $x^2 + 5x + 4$ or $x^2 + x + 4x + 4$ For $x^2 + 5x + 4 - 15 = 35$ or $x^2 + 5x + 4 = 50$ or simpler |
| | OR $(x + 1)(x - 1) + 5(x - 2) = 35$ | | 3 | M1 | For $(x + 1)(x - 1) + 5(x - 2) = 35$ |
| | $x^2 + x - x - 1 + 5x - 10$ | $x^2 + 5x - 11 = 35$ | | B1 A1 | For $x^2 + x - x - 1 + 5x - 10$ or simpler For $x^2 + 5x - 1 - 10 = 35$ |
| | (b) $\frac{-5 \pm \sqrt{5^2 - 4 \times -46}}{2}$ | | 3 | M1 | |
| | $\frac{-5 \pm \sqrt{209}}{2}$ | 4.73 | | M1 A1 | May be implied by an answer of 4.75 For 4.73 or better (4.7284...) Accept 4.73 and -9.73 or better |
| | | | | | Total 6 marks |

| | | | | | |
|----------------------|-----|--|---|----------------|---|
| 18. | (a) | $\frac{9.4}{\sin 123^\circ} = \frac{AC}{\sin 35^\circ}$ $AC = \frac{9.4 \sin 35^\circ}{\sin 123^\circ}$ | 3 | M1 | For 6.43 or better (6.4287...) |
| | | | | M1 | |
| | | 6.43 | | A1 | |
| | (b) | $\frac{1}{2} \times 9.4 \times "6.43" \times \sin x^\circ$ <p>or $\frac{1}{2} \times AB \times "6.43" \times \sin 123^\circ$ or $\frac{1}{2} \times AB \times 9.4 \times \sin 35^\circ$</p> | 3 | M1 B1 | For clear attempt to use " $\frac{1}{2}absinC$ " For $x = 22$ or $AB = 4.2$ or better (4.1987...) appropriate for their form of $\frac{1}{2}absinC$ If M0, award for $x = 22$ or $AB = 4.2$ or better (may be shown on diagram) 11.3 or better (11.3188); ft from (a) |
| | | 11.3 | | A1 | |
| Total 6 marks | | | | | |
| 19. | (a) | $\frac{3}{6} \times \frac{2}{6}$ | 2 | M1 | |
| | | $\frac{6}{36}$ | | A1 | |
| | (b) | $\frac{1}{6} \times \frac{1}{6} + \frac{3}{6} \times \frac{3}{6} + \frac{2}{6} \times \frac{2}{6}$ $= \frac{1}{36} + \frac{9}{36} + \frac{4}{36}$ | 4 | M1 M1 M1 | 1 correct product All 3 correct products Summing at least 2 correct products |
| | | $\frac{14}{36}$ | | A1 | |

| | | | | | |
|----------------------|--|--------------------|----|--|--|
| OR | BB BA BN BA BN BA AB AA AN AA AN AA NB NA NN NA NN NA AB AA AN AA AN AA NB NA NN NA NN NA AB AA AN AA AN AA | 4 | M3 | List of all 36 combinations M2 for 1 omission M1 for 15 or more combinations | |
| | $\frac{14}{36}$ | | | | A1 |
| Total 6 marks | | | | | |
| 20. | (a) | 16 | 1 | B1 cao | |
| | (b) | | 3 | M1 M1 A1 | May be implied by line $x + y = 11$ Accept coordinates ft from candidate's line if first M1 scored, line has negative gradient and there are 3 points of intersection |
| | | ~ -2.3, - 0.3, 2.6 | | | |
| Total 4 marks | | | | | |
| 21. | (a) | 6.5 | 3 | M1 M1 A1 | For $\sqrt{16}$ or 4 or $26^2 \times \frac{157}{2512}$ (42.25) cao |

(b) 4^3 or 64

8320

2 M1
A1

cao

Total 5 marks

22.

$$\frac{2}{x-1} + \frac{x-11}{(x-1)(x+4)}$$
$$\frac{2(x+4) + (x-11)}{(x-1)(x+4)}$$

or

$$\frac{2(x+4)}{(x-1)(x+4)} + \frac{x-11}{(x-1)(x+4)}$$
$$\frac{2x+8+x-11}{(x-1)(x+4)}$$
$$\frac{3x-3}{(x-1)(x+4)}$$
$$\frac{3(x-1)}{(x-1)(x+4)}$$

6 B1

For factorising $x^2 + 3x - 4$

B1 For correct single fraction even if unsimplified, or for correct sum of two fractions with the same denominator ft from incorrect factorisation

B1 For expanding brackets correctly in numerator

B1 For simplifying their numerator

B1 For factorising a correct numerator

$$\frac{3}{(x+4)}$$

B1 cao

SC If no denominator, award 3rd B1 for $2x + 8 + x - 11$ or $2x^2 + 6x - 8 + x^2 - 11x - x + 11$ and 4th B1 for $3x - 3$ or $3x^2 - 6x + 3$

Total 6 marks

TOTAL FOR PAPER: 100 MARKS